

(NEP)

B.Sc. III Semester Degree Examination, February/March - 2023 MATHEMATICS

Ordinary Differential Equations and Real Analysis - I

Time: 3 Hours

Maximum Marks: 60

Instructions to Candidates :

1. Part : A - All questions are compulsory.

2. Part : B - Answer any five full questions.

PART-A

L Answer the following questions.

 $(5 \times 2 = 10)$

a. Solve (4x+3y+1)dx+(3x+2y+1)dy=0.

b. Solve $(p-xy)(p-x^2)(p-y^2)=0$.

c. Evaluate $\frac{1}{D^2 + a^2} \cos ax$.

d. Discuss the convergence of the sequence $\cos^2 n\pi$.

e. Define convergent and divergent of the series.

PART-B

Answer any five full questions.

 $(5 \times 10 = 50)$

IL a. Solve $(\sin x \cos y + e^{2x}) dx + (\cos x \sin y + \tan y) dy = 0$.

b. Solve $x^2p^2 + xyp - 2y^2 = 0$.

III. a. Solve $x^2ydx - (x^3 + y^3)dy = 0$.

b. Solve $y = x + 2 \tan^{-1} P$.

IV. a. Solve $4\frac{d^2y}{dx^2} + 4\frac{dy}{dx} - 3y = e^{2x}$.

b. Solve by method of variation of parameter $\frac{d^2y}{dx^2} + y = \sec x$.



Solve $(D^2 + 3D + 2)y = e^{2x} \sin x$. V.

Verify the condition for integrability $zdx + zdy + [2(x+y) + \sin z]dz = 0$. b.

Prove that the sequence $\left\{\frac{2n+7}{3n+2}\right\}$. VI. a.

is monotonically increasing.

is bounded. ii.

Tends to limit 2/3.

Discuss the convergence of the following sequence. b.

i.
$$1 + \frac{1}{3} + \frac{1}{3^2} + \dots + \frac{1}{3^n}$$
.

ii.
$$\frac{n}{n^2+1}$$
.

Find the limit of the sequence 0.7,0.77,0.777,..... VII. a.

State and prove D'Alembert's ratio test.

Discuss the convergence of the series $\frac{x}{2\sqrt{1}} + \frac{x^3}{3\sqrt{2}} + \frac{x^5}{4\sqrt{3}} + \dots \infty$. b. VIII. a.

Discuss the convergence of the series b.

i.
$$1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots + 0^{\infty}$$
.

Prove that every absolutely convergent series is convergent. ii.



B.Sc. III Semester Degree Examination, February/March 2022 Paper – 3 : MATHEMATICS – III (New)

Time: 3 Hours Max. Marks: 80

Instructions: 1) Part - A: All questions are compulsory.

2) Part - B: Solve any five questions from seven questions.

3) Write the question number correctly.

PART - A

Answer the following questions.

 $(10 \times 2 = 20)$

Define infimum and supremum of the sequence.

2) Test the convergence of the series $\sum \tan \frac{1}{n}$.

3) State Cauchy's Root test.

4) If a series $\sum u_n$ is convergent, then prove that $\lim_{n\to\infty}u_n=0$.

5) Test the convergence or divergence of the series $\frac{1}{1.4} + \frac{1}{2.5} + \frac{1}{3.6} + \dots + \infty$.

6) Find the angle between the radius vector and the tangent for the curve $r = a (1-cos\theta)$.

7) For the cardioid $r = a (1 - \cos\theta)$, show that $2ap^2 = r^3$.

8) Find the length of polar subtangent and polar subnormal at the point $\theta = \frac{\pi}{6}$ for the curve $r = acos2\theta$.

9) Evaluate ∫ secⁿ x dx.

10) Evaluate $\int_{0}^{\pi/2} \sin^4 x \cos^2 x \, dx$

PART - B

Answer any five complete questions.

 $(5 \times 12 = 60)$

II. 11) State and prove limit form of comparision test.

12) Discuss the convergence of the series $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5} + \dots$



- III. 13) State D'Alembert's test and test the convergence of the series $\sum \frac{2^{n-1}}{3^n+1}$.
 - 14) Sum the series by C+is method $\cos \alpha + \cos (\alpha + \beta) + \cos (\alpha + 2\beta) + + to n terms.$
- IV.15) Find the angle between the curves at their point of intersection $r = a (1 \cos \theta)$, $r = 2a \cos \theta$.
 - 16) Show that the following pairs of curves intersect orthogonally $r^n = a^n cosn\theta$, $r^n = b^n sinn\theta$.
- V. 17) Derive the length of perpendicular from the pole to the tangent at a point to the curve.
 - 18) Show that for the curve $r^2 = a^2 \sec 2\theta$, the length of the perpendicular from the pole to tangent is $a\sqrt{\cos 2\theta}$.
- VI. 19) Find the Pedal equation of the curve $r^2 = a^2 \cos 2\theta$.
 - 20) Show that the curve $r^2 = a^2 cos 2\theta$ and $r = a (1 + cos \theta)$ intersect at an angle $3 sin^{-1} \left(\frac{3}{4}\right)^{\frac{1}{4}}$.
- VII. 21) Find the reduction formula for $\int_{0}^{\pi/2} \cos^{n} x \, dx$.
 - 22) Evaluate:
 - i) $\int_{0}^{\pi} x \sin^{4} \theta \cos^{6} \theta d\theta$
 - ii) Show that $\int\limits_{0}^{\pi/2} \sin^4 x \cos^2 x dx = \frac{\pi}{32}$.
- VIII. 23) Evaluate:

$$i) \int_0^4 x^3 \sqrt{4x - x^2} dx$$

ii)
$$\int_{\pi/4}^{\pi/2} \cot^5 x dx \cdot$$

24) Evaluate $\int_{0}^{\pi/2} \frac{dx}{(a^2 \cos^2 x + b^2 \sin^2 x)^2}$ using Leibnitz's rule of differentiation under integral sign.



B.Sc. III Semester Degree Examination, February/March 2022 MATHEMATICS

Paper - 3.1: Vector Algebra and Solid Geometry (Old)

Time: 3 Hours

Max. Marks: 60

Instructions: 1) Answer all Sections.

2) Write the question number correctly.

SECTION - A

I. Answer any ten of the following:

- 1) Find the unit vector coplanar with \vec{a} and \vec{b} and perpendicular to \vec{c} where $\vec{a} = 2i j + k$, $\vec{b} = i + 2j k$ and $\vec{c} = 2i + 3j$.
- 2) Show that $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b}) = 0$.
- 3) If \vec{a} , \vec{b} , \vec{c} and \vec{a}' , \vec{b}' , \vec{c}' are reciprocal system of vectors prove that $\vec{a}'(\vec{a}+\vec{b})+\vec{b}'(\vec{b}+\vec{c})+\vec{c}'(\vec{c}+\vec{a})=3$.
- 4) Find the distance between the points A = (-2, 3, 5), B = (1, 2, 3).
- 5) Find the co-ordinates of the point that divides the line joining the points (2, -3, 1) and (3, 4, -5) in the ratio 1: 3.
- 6) A line makes angle of 45° and 60° with the positive axis of x and y respectively. What angle does it make with positive axis of z?
- 7) Find the area of the triangle whose vertices are (6, -1, 6), (6, -4, 9), (10, 0, 7).
- 8) Find the angle between the planes 6x 3y 2z 7 = 0 and x + 2y + 2z + 9 = 0.
- 9) Find the length of perpendicular from (1, 3, 4) to the plane 2x y + z + 3 = 0.



- 10) Find the equation of the plane passing through the points (0, 1, 1), (1, 1, 2) and (-1, 2, -2).
- 11) Find the equation of the plane bisecting the angle between the planes 3x 4y + 5z 3 = 0 and 5x + 3y 4z 9 = 0.
- 12) Show that the line $\frac{x-1}{1} = \frac{y+1}{-1} = \frac{z-3}{1}$ and $\frac{x-2}{2} = \frac{y-4}{1} = \frac{z-6}{3}$ are coplanar.

II. Answer any two of the following:

 $(2 \times 5 = 10)$

- 13) Show that $i \times (\overrightarrow{a} \times i) + j \times (\overrightarrow{a} \times j) + k \times (\overrightarrow{a} \times k) = 2\overrightarrow{a}$.
- 14) If \vec{a} , \vec{b} , \vec{c} are any three vectors, then prove that

$$\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{c}) \vec{b} - (\vec{a} \cdot \vec{b}) \vec{c}$$

- 15) If $\vec{a} = i + 2j 2k$, $\vec{b} = -i + 2j + k$, $\vec{c} = i 2j + 2k$, find $(\vec{a} \times \vec{b}) \times \vec{c}$ and $\vec{a} \times (\vec{b} \times \vec{c})$.
- 16) If \vec{a} , \vec{b} , \vec{c} and $\vec{a'}$, $\vec{b'}$, $\vec{c'}$ are reciprocal system of vectors, then show that

$$\sum \left(\overrightarrow{a'} \times \overrightarrow{b'} \right) = \frac{\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}}{\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c} \right]} \text{ where } \left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c} \right] \neq 0.$$

III. Answer any three of the following :

- 17) Find the direction cosines of two lines which are connected by the relation l 5m + 3n = 0 and $7l^2 + 5m^2 3n^2 = 0$.
- 18) Show that the acute angle between two lines whose direction cosines are given by the relations l + m + n = 0 and 2lm + 2nl mn = 0 is 60° .



- 19) Find the value of 'a' such that the points A(3, 2, 1), B(4, a, 5), C(4, 2, -2) and D(6, 5, -1) are coplanar.
- 20) Find the volume of the tetrahedron ABCD, where A = (1, 0, -1), B = (2, 1, -1), C = (1, 0, 2) and D = (2, 1, 0).
- 21) Find the equation of the plane passing through the points A(1, 1, 1) and perpendicular to the planes $\vec{r} \cdot (1, -3, 5) + 1 = 0$ and $\vec{r} \cdot (3, -1, 7) = 3$.

SECTION - D

IV. Answer any three of the following:

- 22) Find the symmetrical form of the lines of intersection of the planes, 2x + 3y + 5z 1 = 0 = 3x + y z + 2.
- 23) Find the angle between the line $\frac{x-3}{2} = \frac{y+1}{-1} = \frac{z+4}{3}$ and the plane 2x + 3y z 4 = 0.
- 24) Find the equation of the plane containing the line $\frac{x+2}{1} = \frac{y-3}{2} = \frac{z+4}{-3}$ and passing through the point (1, 3, 2).
- 25) Show that the lines 3x y z 16 = 0 = 2x 3y 2z 19 and 2x + 4y + z + 12 = 0 = x 2y z 13 are coplanar.
- 26) Find the shortest distance between the lines $\frac{x-3}{1} = \frac{y-4}{-2} = \frac{z+2}{-1}$ and 3x-y-10=0=2x-z-4.



B.Sc. III Semester Degree Examination, March/April - 2021 MATHEMATICS-III

Paper: 3

(New)

Time: 3 Hours

Maximum Marks: 80

Instructions to Candidates:

- 1) PART-A All questions are compulsory.
- PART B Solve any Five questions from Seven questions.
- Write the question number correctly.

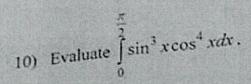
PART - A

Answer the following questions.

- 1) Define Infimum and Suprimum of the sequence.
- 2) State P Series.
- 3) State Raabe's Test.
- 4) Discuss the convergence of the series $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5} + \dots$
- 5) Test the convergence of $\sum \frac{1}{\sqrt{n}} \tan \frac{1}{n}$.
- 6) Find the angle between the radius vector and the tangent for the curve $r = a(1 \cos \theta)$.
- 7) For the curve $r = a\theta$ show that $p = \frac{r^2}{\sqrt{r^2 + a^2}}$.
- 8) Find the ratio of the Polar subnormal to the polar subtangent for the curve $r = ae^{b\theta^2}$.

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VI.



PART - B

(5×12≈6

Answer any Five complete questions.

- State and prove De Alembert's ratio test. 11.
 - 12) Examine the convergence of the series $1 + \frac{1}{2} + \frac{1.3}{2.4} + \frac{1.3.5}{2.4.6} + \dots$
- III. 13) State Cauchy's root test and hence test the convergence of the sen $\sum \left(\frac{nx}{n+1}\right)^n$
 - Sum the series by C+ is method $\cos \alpha + \cos (\alpha + 2\beta) + \dots + \tan \beta$
- Show that the following pair of curves intersect orthogonally $r = a\theta$, r = 0
 - 16) For the curve cardiod $r = a(1 + \cos \theta)$ Show that $2ap^2 = r^3$.
- V. (17) Derive the length of the perpendicular from the pole to the tangent at a po to the curve.
 - Find the pedal equation of the curve $r = ae^{\theta \cot \alpha}$ (i)
 - Find the angle between the radius vector and the tangent for the cur-

$$r^2 = a^2 \cos 2\theta$$
 at $\theta = \frac{\pi}{6}$



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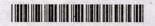
- VI. 19) Show that the curve $r^2 = a^2 \sec 2\theta$ the length of the perpendicular from the pole to the tangent $a\sqrt{\cos 2\theta}$.
 - 20) Show that the angle between the normal at any point (r,θ) on the curve $r'' = a'' \cos n\theta$, and the initial line is $(n+1)\theta$.
- VII. 21) Find the reduction formula for $\int \sec^n x dx$.
 - 22) Evaluate (i) $\int_{0}^{1} x^{3/2} \sqrt{(1-x)^3} dx$

(ii)
$$\int_{0}^{\infty} \frac{x}{\left(4+x^2\right)^{\frac{3}{2}}} dx$$

VIII.23) Evaluate (i) $\int_{0}^{\pi} x \sin^{7} x \cos^{2} x dx$

(ii)
$$\int_{0}^{\pi/4} \tan^4 x \, dx = \frac{3\pi - 8}{12}$$

24) Compute the definite integral $\int_0^1 \frac{x^{\alpha} - 1}{\log x} dx$, where ' α ' is a parameter using Leibnitz's rule of differentiation under integral sign.



B.Sc. III Semester Degree Examination, March/April - 2021 MATHEMATICS

Vector Algebra and Solid Geometry

Paper - 3.1 (Old)

Time: 3 Hours

Maximum Marks: 60

Instructions to Candidates:

- 1. Answer all Sections.
- 2. Write the question number Correctly.

SECTION - A

I. Answer any Ten of the following:

- 1) Define collinear and coplanar vectors.
- 2) Show that $i \times (j \times k) + j \times (k \times i) + k \times (i \times j) = 0$
- 3) Find the unit vector coplanar with \vec{b} and \vec{c} and perpendicular to \vec{a} where $\vec{a} = 2\mathbf{i} + \mathbf{j} \mathbf{k}$, $\vec{b} = \mathbf{i} 2\mathbf{j} + 2\mathbf{k}$ and $\vec{c} = 3\mathbf{i} \mathbf{j} + 2\mathbf{k}$.
- 4) Show that three points (-2,3.5), (1,2,3) and (7,0,-1) are collinear.
- 5) Find the ratio in which the point (5,4,-6) divides the line Joining the points (3,2,-4) and (9,8,-10)
- 6) If α , β , γ are the angle made by a line with the co-ordinates axes. Show that $\cos 2\alpha + \cos 2\beta + \cos 2\gamma + 1 = 0$.
- 7) Using the direction ratio show that the lines AB and CD are parallel, where A = (1, 2, 3), B = (4, -3, 6), C = (-1, 2, -2) and D = (2, -3, 1).
- 8) Find the angle between the planes 6x-3y-2z-7=0 and x+2y+2z+9=0.
- 9) Find the equation of the plane passing through the points (0,1,1),(1,1,2) and (-1,2,-2).



- 10) Find the equation of the line passing through the point A(1,-1,1) and parallel to the vector i j + k.
- 11) Find the angle between the plane x-3y+2z-7=0 and the line x-2y+3z+1=0=3x+y+2z+2.
- 12) Show that the lines are coplanar $\frac{x-1}{1} = \frac{y+1}{-1} = \frac{z-3}{1}$ and $\frac{x-2}{2} = \frac{y-4}{1} = \frac{z-6}{3}$.

SECTION - B

II. Answer any Two of the following:

 $(2 \times 5 = 10)$

- 13) Find the unit vector co-planar with \vec{a} and \vec{b} but perpendicular to \vec{c} , where $\vec{a} = \mathbf{i} + \mathbf{j} 2\mathbf{k}$, $\vec{b} = -\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ and $\vec{c} = \mathbf{i} 2\mathbf{j} + 2\mathbf{k}$.
- 14) Show that $i \times (\vec{a} \times i) + j \times (\vec{a} \times j) + k \times (\vec{a} \times k) = 2\vec{a}$
- 15) Find a set of vectors reciprocal to the set of vectors $\vec{a} = 2\hat{i} + 3\hat{j} \hat{k}$, $\vec{b} = 3\hat{i} \hat{j} + \hat{k}$.
- 16) If \vec{a} , \vec{b} , \vec{c} and \vec{a}' , \vec{b}' , \vec{c}' are reciprocal system of vectors then show that:
 - i) $\vec{a}.\vec{a}' + \vec{b}.\vec{b}' + \vec{c}.\vec{c}' = 3$
 - ii) $\vec{a}' \times \vec{b}' + \vec{b}' \times \vec{c}' + \vec{c}' \times \vec{a}' = \frac{\vec{a} + \vec{b} + \vec{c}}{\left[\vec{a} \ \vec{b} \ \vec{c}\right]}; (\vec{a}, \vec{b} \ \vec{c}) \neq 0$

SECTION - C

III. Answer any Three of the following:

- 17) Find the direction cosines of the two lines which are connected by the relation l-5m+3n=0 and $7l^2+5m^2-3n^2=0$.
- 18) Find the angle between the two lines whose direction cosines satisfy the equation l+m+n=0 and 2l+2m-nm=0



- 19) Find the volume of the tetrahedron ABCD, where A(1,0,-1), B(2,1,-1)C(1,0,2) and D(2,1,0).
- 20) Find the equation of the plane passing through the point A(1,1,1) and perpendicular to the planes $\vec{r}.(1,-3,5)+1=0$ and $\vec{r}.(3,-1,7)=3$
- 21) Find the angle between the diagonals of a cube.

SECTION - D

IV. Answer any Three of the following:

- 22) Show that the points (0,-1,0)(2,1,-1)(1,1,1) and (3,3,0) are coplanar. Find the equation of the plane passing through the points.
- 23) Find the symmetrical form of the lines of intersection of the planes 2x+3y+5z-1=03x+y-z+2=0
- 24) Find the equation of the plane containing the line $\frac{x+2}{1} = \frac{y-3}{2} = \frac{z+4}{-3}$ and passing through the point (1, 3, 2).
- 25) Derive the condition for a line to lie on a plane both in vector and cartesian form.
- 26) Find the shortest distance between the lines $\frac{x-3}{1} = \frac{y-4}{-2} = \frac{z+2}{-1}$ and 3x-y-10=0 2x-z-4=0

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B.Sc. III Semester Degree Examination, Oct./Nov. - 2019

MATHEMATICS

MATHEMATICS-III

PAPER-3

Time: 3 Hours

Maximum Marks:80

Instructions to Candidates:

1) Part-A: All questions are compulsory.

- 2) Part-B: Solve any Five questions from seven questions.
- 3) Write the question number correctly.

PART - A

Answer the following questions.

- 1. Define convergence and divergence of a sequence.
- 2. Test the convergence of the series $\sum \frac{1}{\sqrt[3]{n}} \tan \frac{1}{n}$
- 3. State Raabe's Test.
- 4. If the series $\sum u_n$ is convergent then prove that $\lim_{n\to\infty} u_n = 0$
- 5. Examine the following series for convergence

$$\frac{1}{\sqrt{1}+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} + ----$$

- 6. Find the angle between the radius vector and the tangent for the curve $r = a(1 + \sin \theta)$ at $\theta = \pi/6$.
- 7. For the curve $r = a\theta$, show that $p = \frac{r^2}{\sqrt{r^2 + a^2}}$.
- 8. Find the ratio of the polar sub normal to the polar subtangent for the curve $r = ae^{b\theta^2}$
- 9. Define reduction formula of the integral and Evaluate $\int_0^{\pi} x \sin^8 x dx$.
- 10. Find the value of $\int_0^{\pi/2} \tan^5 x \, dx$

PART - B

Answer any Five complete questions.

11. State and prove limit form of comparision test. 12. Discuss the convergence of the following series $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{1}{3.4.5}$ 11.

III. 13. Examine the convergence of the series $\frac{2!}{3} + \frac{3!}{3^2} + \frac{4!}{3^3} + \cdots$ by D' Alember ratio test.

14. Sum the series (by C+iS method) $\sin \alpha + \sin (\alpha + \beta) + \sin (\alpha + 2\beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta) + \sin (\alpha + \beta) = \sin (\alpha + \beta)$

terms

15. Find the angle of intersection of each of the following pairs of curve. IV. $r = (\sin \theta + \cos \theta), r = 2\sin \theta$

16. Show that the following pair of curves intersect orthogonally $r = a(1 + \sin \theta), r = b(1 - \sin \theta).$

17. Derive the length of the perpendicular from the pole to the tangent at a point to the V. curve.

18. For the curve cardiod $r = a(1-\cos\theta)$ show that $2ap^2 = r^3$

VI. 19. Find the pedal equation of the following curve $a^2 = r^2 \cos 2\theta$

20. Show that the angle between the normal at any point (r,θ) on the curvi $r'' = a'' \cos n\theta$, and the initial line is $(n+1)\theta$

Find the reduction formula for $\int \sec^n x \, dx$

22. Evaluate:

i)
$$\int_0^4 x^3 \sqrt{4x - x^2} \, dx$$

ii)
$$\int_0^1 x^4 (1-x)^{3/2} dx.$$

VIII.23. Show that

i)
$$\int_{\pi}^{\pi} \frac{\sin^4 \theta}{1 + \cos \theta^2} d\theta = \frac{3\pi}{4}$$

ii) $\int_0^{\pi/4} Sin^4 x.\cos^2 2 dx = \pi/32$

Compute the definite integral $\int_0^1 \frac{x^{\alpha}-1}{\log x} dx$, Where '\alpha' is a parameter. us leibnitz's rule differentiation under integral sign

(NEP)

B.Sc. III Semester Degree Examination, February/March - 2023 MATHEMATICS

Ordinary Differential Equations and Real Analysis - I

Time: 3 Hours

Maximum Marks: 60

Instructions to Candidates :

Part : A - All questions are compulsory.

Part : B - Answer any five full questions. 2.

PART-A

Answer the following questions. L

 $(5 \times 2 = 10)$

Solve (4x+3y+1)dx+(3x+2y+1)dy=0.

Solve $(p-xy)(p-x^2)(p-y^2)=0$

Evaluate $\frac{1}{D^2 + a^2} \cos ax$.

Discuss the convergence of the sequence $\cos^2 n\pi$. d.

Define convergent and divergent of the series. e.

PART-B

Answer any five full questions.

(5×10=50)

Solve $\left(\sin x \cos y + e^{2x}\right) dx + (\cos x \sin y + \tan y) dy = 0$. II. a.

b. Solve $x^2p^2 + xvp - 2v^2 = 0$.

a. Solve $x^2ydx - (x^3 + y^3)dy = 0$. III.

b. Solve $y = x + 2 \tan^{-1} P$.

IV. a. Solve $4\frac{d^2y}{dx^2} + 4\frac{dy}{dx} - 3y = e^{2x}$.

Solve by method of variation of parameter $\frac{d^2y}{dx^2} + y = \sec x$. b.

MINISHMA

Solve $(D^2 + 3D + 2)y = e^{2x} \sin x$. V. a

Verify the condition for integrability $zdx + zdy + [2(x+y) + \sin z]dz = 0$. b.

Prove that the sequence $\left\{\frac{2n+7}{3n+2}\right\}$. a. VI.

is monotonically increasing. i.

is bounded. ii.

Tends to limit 2/3.

Discuss the convergence of the following sequence.

i.
$$1 + \frac{1}{3} + \frac{1}{3^2} + \dots + \frac{1}{3^n}$$
.

ii.
$$\frac{n}{n^2+1}$$
.

Find the limit of the sequence 0.7,0.77,0.777,..... VII. a.

State and prove D'Alembert's ratio test. b.

Discuss the convergence of the series $\frac{x}{2\sqrt{1}} + \frac{x^3}{3\sqrt{2}} + \frac{x^5}{4\sqrt{3}} + \dots \infty$. VIII. a.

b. Discuss the convergence of the series

i.
$$1-\frac{1}{2}+\frac{1}{3}-\frac{1}{4}+\dots+0\infty$$
,

Prove that every absolutely convergent series is convergent. ii.